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Enhanced group structure of waves in ice - Linear or nonlinear process?

Motivation:

Previous case study
in pancake ice

(Thomson et al 2019, JGR):

High frequency wave attenuation

→ narrow band

Linear superposition

→ Strong group structure

Here: new study, 4 year record, including thick first year ice

Definitions: Wave parameters

Significant wave height

$$H_s = 4\sqrt{m_0}$$

Spectral moments

$$m_n = \int \omega^n S(\omega) d\omega$$

Dominant frequency

$$\omega_p = \frac{\int \omega S(\omega)^4 d\omega}{\int S(\omega)^4 d\omega}$$

Spectral bandwidth

$$\nu = \left(\frac{m_0 m_2}{m_1^2} - 1 \right)^{\frac{1}{2}}$$

Steepness

$$\varepsilon = k_p H_s / 2$$

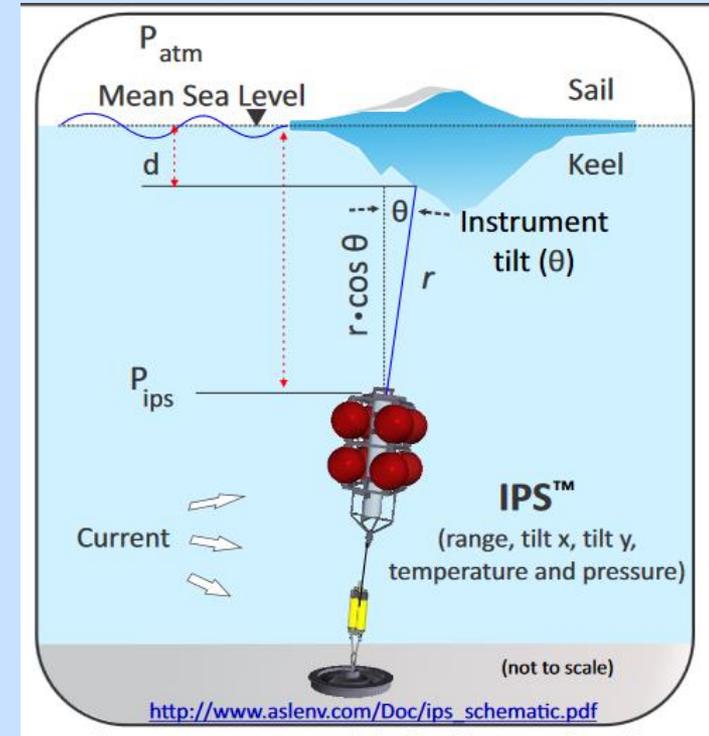
Group factor

$$GF = \frac{\sigma_{SWH}}{\langle SWH \rangle}$$

Smoothed Instantaneous **Wave Energy History** $SWH = Q * \eta^2$
(wave envelope)

(Q: Bartlett window length $2T_p$)

Observations: surface elevation (various ice conditions)

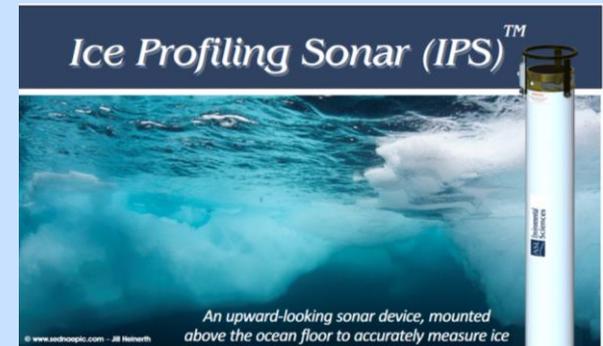


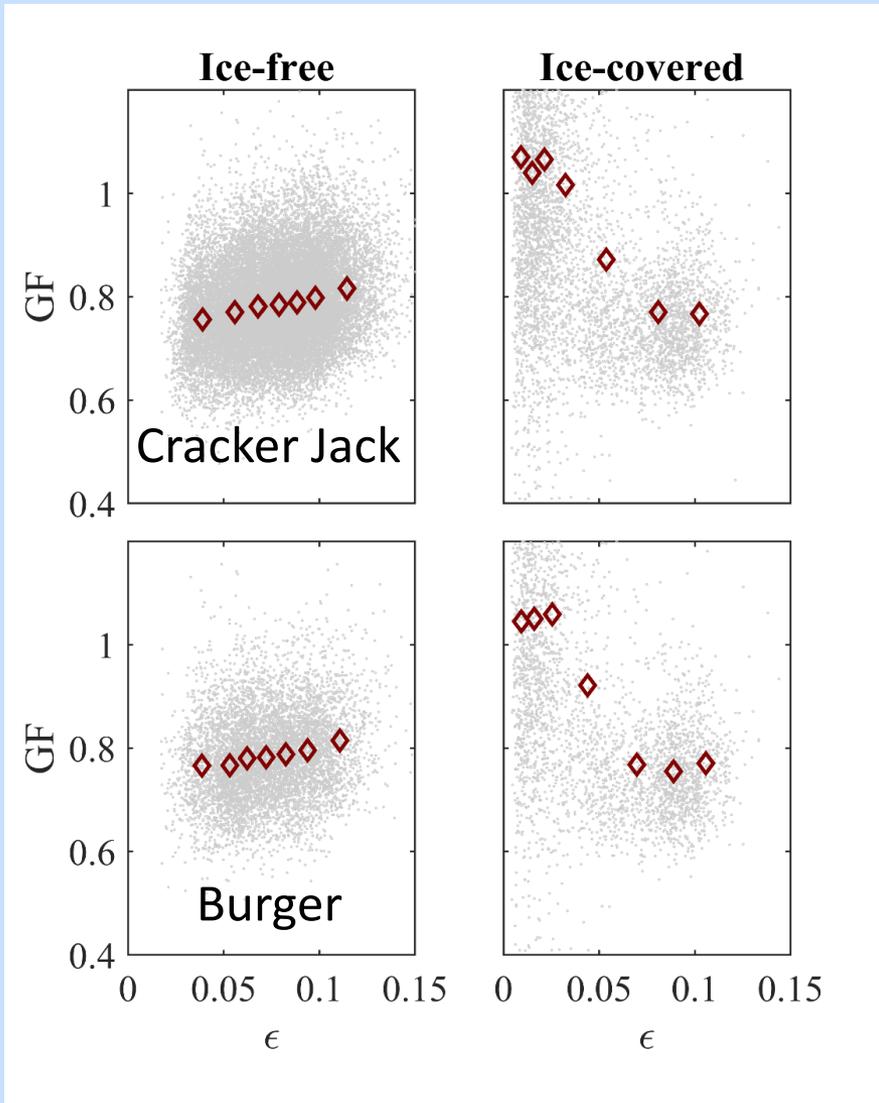
Observations 2010 – 2015

2 sites: Burger and Cracker Jack, ~47m depth

- Range to surface at 0.5 Hz (some 1 Hz),

→ 1d 'surface elevation' time series
(inverted echosounder range)





Ice free:

- Lower GF
- **Steeper waves**
→ more pronounced groups

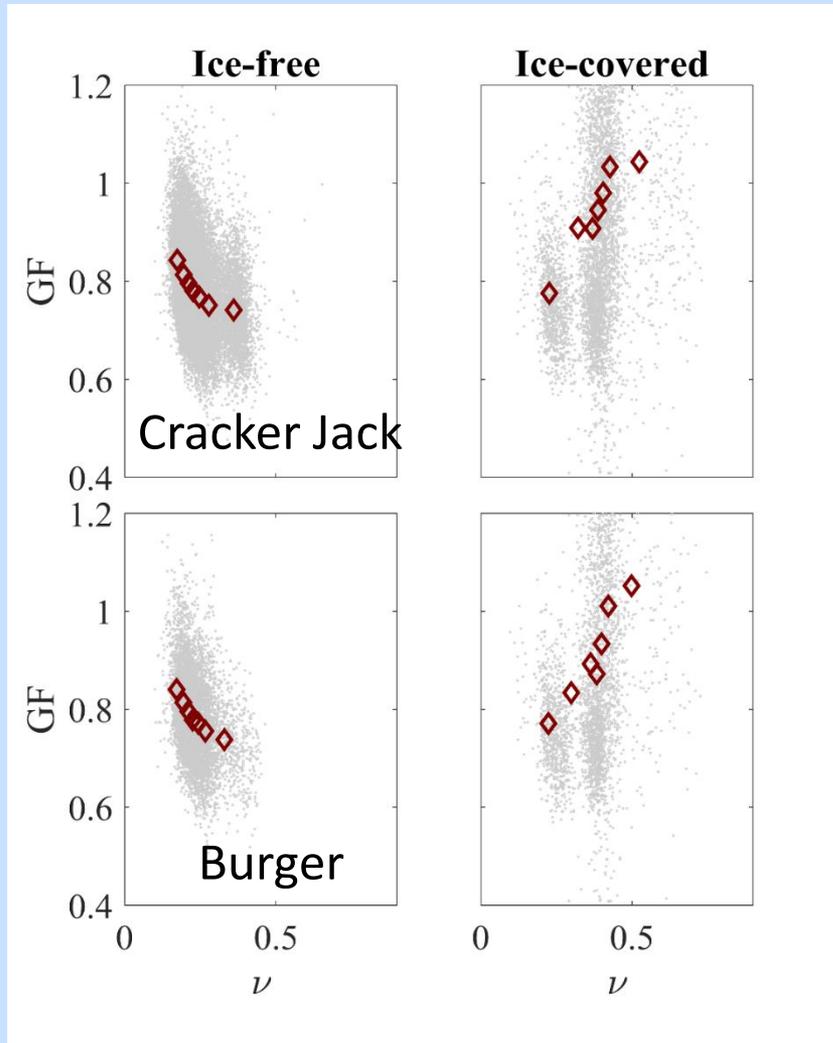
Ice covered:

- Higher GF
- **Steeper waves**
→ less pronounced groups

Similar steepness in ice and ice-free
(despite lower Hs)

→ Attenuation of longer waves (?)
Or change in dispersion relation (?)

(Note: in pancake ice: GF highest in ice, decreasing with steepness)



Ice free:

- **Narrow-banded waves**
→ more pronounced groups

Ice covered:

- **Broad-banded waves**
→ more pronounced groups

Similar bandwidth in ice or ice-free

→ Why?

(would expect high-frequency attenuation in ice)

→ linear: narrow band)

(Note: in pancake ice: GF highest in ice, decreasing with bandwidth)

Group factor – bandwidth: nonlinear process

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Original Russian Text © V.G. Polnikov, I.V. Lavrenov, 2007, published in *Okeanologiya*, 2007, Vol. 47, No. 3, pp. 363–373.

MARINE
PHYSICS

Calculation of the Nonlinear Energy Transfer through the Wave Spectrum at the Sea Surface Covered with Broken Ice

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Note: Spectral bandwidth defined omni-directional, but group generation effective in unidirectional waves

Ice reduces nonlinear 4-wave transfer

but enhanced transfer to high frequencies

(compensates for high frequency attenuation: $\rightarrow n_{\text{ice}} \sim n_{\text{water}}$)

→ High frequency spreads to lateral directions

→ Waves in dominant direction more “narrow-banded”

→ Increase in group factor

Process less pronounced in narrow band wave field

Broad-banded waves → high frequency lateral spread → more pronounced groups

Wave groups in ice: linear or nonlinear?

| | | |
|-------------------|--|--------------------------------|
| <u>Thin ice:</u> | Group factor decreasing with bandwidth | linear ^{a)} |
| <u>Thick ice:</u> | Group factor increasing with bandwidth | nonlinear ^{b)} |

**Ice enhances nonlinear 4-wave transfer to high frequencies
→ Lateral spread → more groups in dominant direction**

Spectral parameter $\leftarrow \rightarrow$ groupiness:

Opposite behaviour in thick ice vs. open water

a) Thomson et al, 2019

b) This study. Consistent with nonlinear mechanism suggested in Collins et al, 2015

References:

Collins, C.O., W.E. Rogers, A. Marchenko, and A. V. Babanin, 2015: *'In situ measurements of an energetic wave event in the Arctic marginal ice zone'*. Geophys. Res. Lett.,42, 1863–1870

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Thomson, J., J. Gemmrich, W. E. Rogers, C. O. Collins, and F. Ardhuin, 2019: *'Wave groups observed in pancake sea ice'*. J. Geophys. Res.124, 7400-7411

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